

# LAYERED TYPES

Combining Dependent and Independent Type Systems

TYPES'23, Valencia

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# FOREWORD

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- This talk focusses on
  - High Level Concepts 
  - Implementation

# MOTIVATION

Lukas Abelt, Alcides Fonseca

- Original Idea comes from challenges in Liquid Types:
  - Composability
  - Reusability
  - Error-Detection

## Untyped

```
x = 100
-- Do something with x
x = -10
```

## Typed

```
x :: Int
x = 100
-- Do something with x
x = -10
```

## Liquid Typed

```
{-@ x :: { v:Int | v > 0} @-}
x :: Int
x = 100
-- Do something with x
x = -10 -- ERROR with liquid types
```

# LAYERED TYPES – MOTIVATION

Lukas Abelt, Alcides Fonseca

## Before

```
{-@ type OrderedList = { v:[Int] | len(v) > 0
                        && all(i,j | i<j => v[i]<v[j]) } @-}
{-@ type PositiveList = { v:[Int] | len(v) > 0
                        && all( i | v[i] > 0 ) } @-}

{-@ foo :: OrderedList → Int @-}
foo :: [Int] → Int

{-@ x :: PositiveList @-}
x :: [Int]

foo(x) = ... -- Perform some complicated operation
```

# LAYERED TYPES – MOTIVATION

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Before

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{-@ type OrderedList = { v:[Int] | len(v) > 0
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{-@ foo :: OrderedList → Int @-}
foo :: [Int] → Int

{-@ x :: PositiveList @-}
x :: [Int]

foo(x) = ... -- Perform some complicated operation
```

```
Error: type of 'x' is not compatible with liquid type:
{ v:[Int] | len(v) > 0 && all(i,j | i<j ⇒ v[i] < v[j]) }
```

# LAYEREDTYPES – MOTIVATION

Lukas Abelt, Alcides Fonseca

After

```
{-@ layer NonEmpty = { v:[Int] | len(v) > 0 } @-}
{-@ layer Ordered = { v:[Int] | all( i,j | i<j =>
                                v[i] < v[j] ) } @-}
{-@ layer Positive = { v:[Int] | all( i | v[i] > 0 ) } @-}

{-@ foo :: { NonEmpty && Ordered } → Int @-}
foo :: [Int] → Int

{-@ x :: { NonEmpty && Positive } @-}
x :: [Int]

foo(x) = ... -- Perform some complicated operation
```

# LAYEREDTYPES – MOTIVATION

Lukas Abelt, Alcides Fonseca

After

```
{-@ layer NonEmpty = { v:[Int] | len(v) > 0 } @-}  
{-@ layer Ordered = { v:[Int] | all( i,j | i<j =>  
                                v[i] < v[j] ) } @-}  
{-@ layer Positive = { v:[Int] | all( i | v[i] > 0 ) } @-}  
  
{-@ foo :: { NonEmpty && Ordered } -> Int @-}  
foo :: [Int] -> Int  
  
{-@ x :: { NonEmpty && Positive } @-}  
x :: [Int]  
  
foo(x) = ... -- Perform some complicated operation
```

**Error:** type of 'x' is not compatible with layer Ordered

# LAYERED TYPES – MOTIVATION

Lukas Abelt, Alcides Fonseca

# LAYEREDTYPES – MOTIVATION

Lukas Abelt, Alcides Fonseca

- Applying this to Liquid Types is nice



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- Applying this to Liquid Types is nice
- But can't we go bigger?
  - Similar problems when combining type systems
  - No unified tooling

# LAYERED TYPES – MOTIVATION

Lukas Abelt, Alcides Fonseca

- Applying this to Liquid Types is nice
- But can't we go bigger?
  - Similar problems when combining type systems
  - No unified tooling
- Can we build something “good”?

# LAYEREDTYPES – VISION

Lukas Abelt, Alcides Fonseca



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Lukas Abelt, Alcides Fonseca

- Incremental Verification
  - Layers build on top of each other
  - Can be verified individually

# LAYERED TYPES – VISION

Lukas Abelt, Alcides Fonseca

- Incremental Verification
  - Layers build on top of each other
  - Can be verified individually
- Separation of Concerns
  - Each Layer is independent
  - Easier to develop, verify and test
  - Error-Detection might be easier

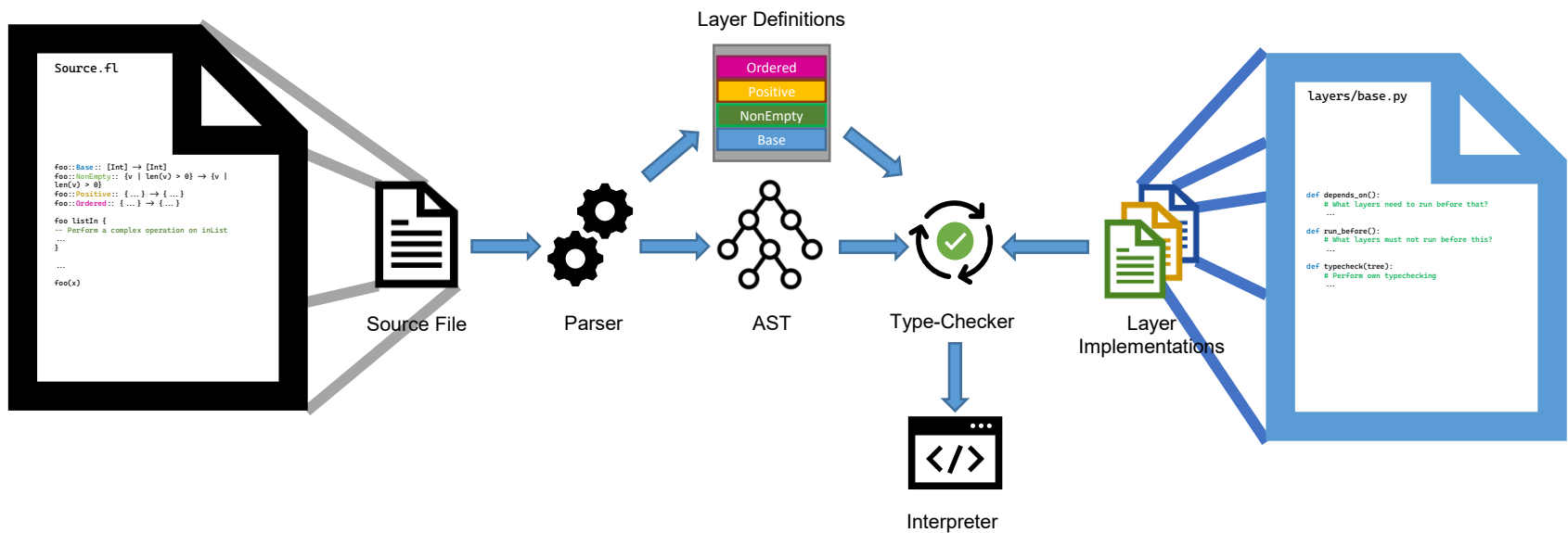
# LAYERED TYPES – VISION

Lukas Abelt, Alcides Fonseca

- Incremental Verification
  - Layers build on top of each other
  - Can be verified individually
- Separation of Concerns
  - Each Layer is independent
  - Easier to develop, verify and test
  - Error-Detection might be easier
- Modularity
  - Existing Layers can be reused
  - Layers can be composed arbitrarily

# LAYERED TYPES – ARCHITECTURE

Lukas Abelt, Alcides Fonseca



# LAYEREDTYPES – SOURCE CODE

Lukas Abelt, Alcides Fonseca

factorial.fl

```
fac x {  
  let cond := (x == 0) in {  
    if cond then {  
      1  
    } else {  
      x * fac (x - 1)  
    }  
  }  
}  
  
x := fac(5)  
print(x)  
  
x
```



# LAYEREDTYPES – LAYERS

Lukas Abelt, Alcides Fonseca

layers.fl

```
X :: LayerA :: ...
X :: LayerB :: ...
X :: LayerC :: ...
X :: LayerD :: ...

X := 42
X
```

layer.py

```
def depends_on():
    # What layers need to run before that?
    ...

def run_before():
    # What layers must not run before this?
    ...

def typecheck(tree):
    # Perform own typechecking
    ...
```

# LAYEREDTYPES – LAYERS

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LayerA.py

```
def depends_on():
    return {}
```

LayerB.py

```
def depends_on():
    return {"LayerA"}
```

LayerC.py

```
def depends_on():
    return {"LayerA"}
```

LayerD.py

```
def depends_on():
    return {"LayerB", "LayerC"}
```

# LAYEREDTYPES – LAYERS

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X := 42
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LayerA.py

```
def depends_on():
    return {}
```

LayerB.py

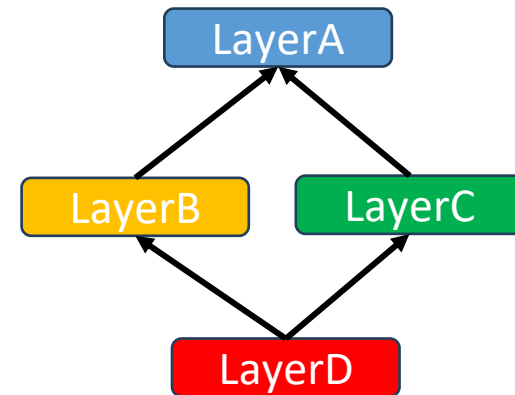
```
def depends_on():
    return {"LayerA"}
```

LayerC.py

```
def depends_on():
    return {"LayerA"}
```

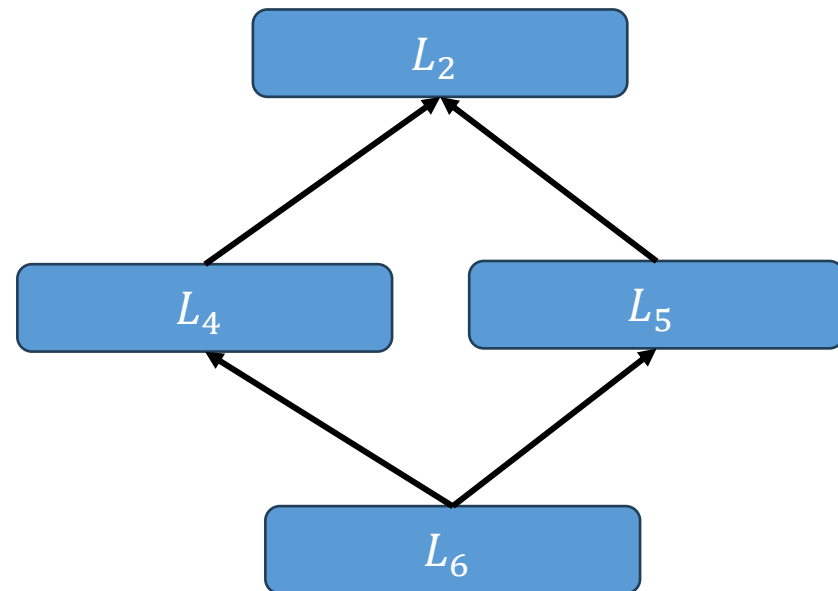
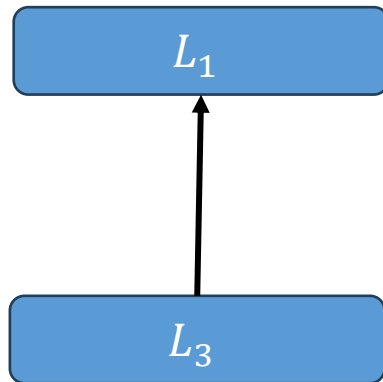
LayerD.py

```
def depends_on():
    return {"LayerB", "LayerC"}
```



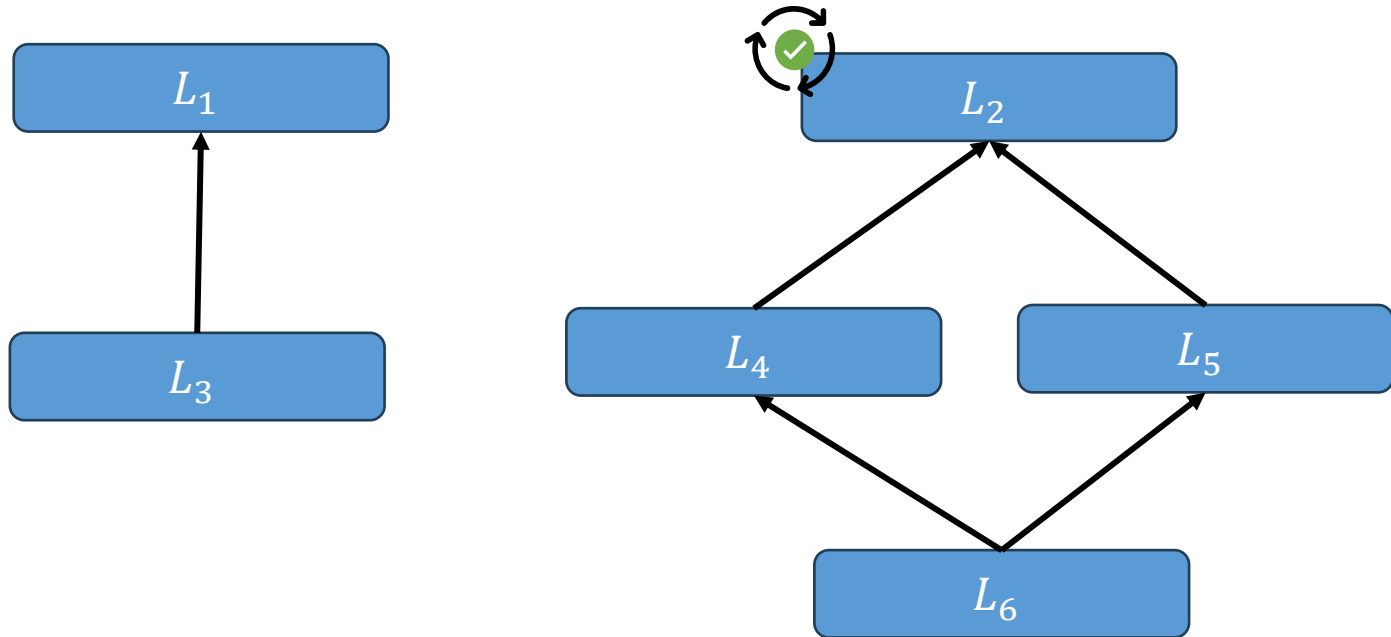
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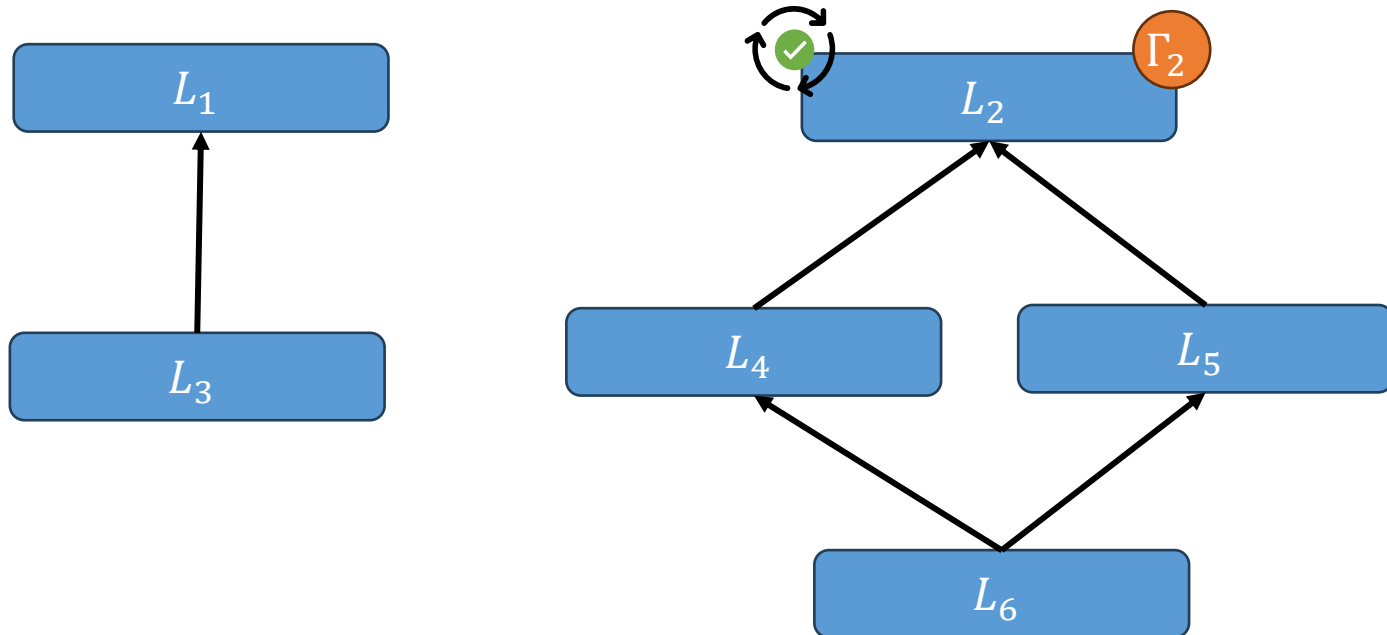
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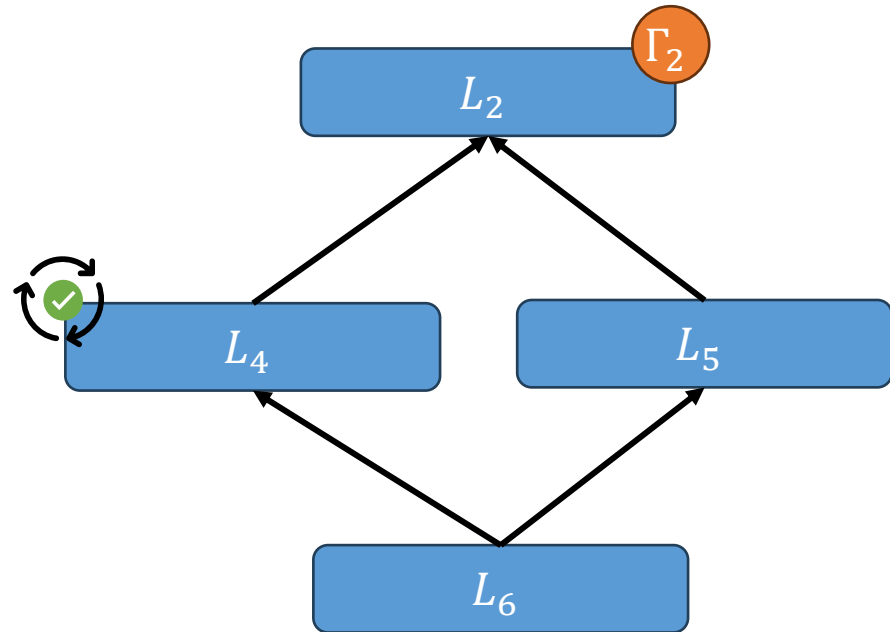
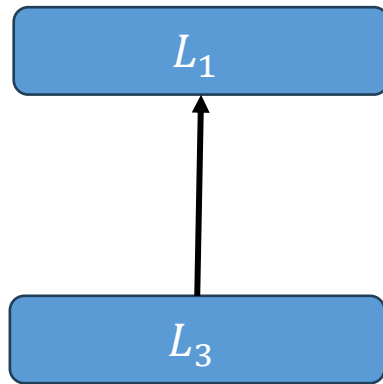
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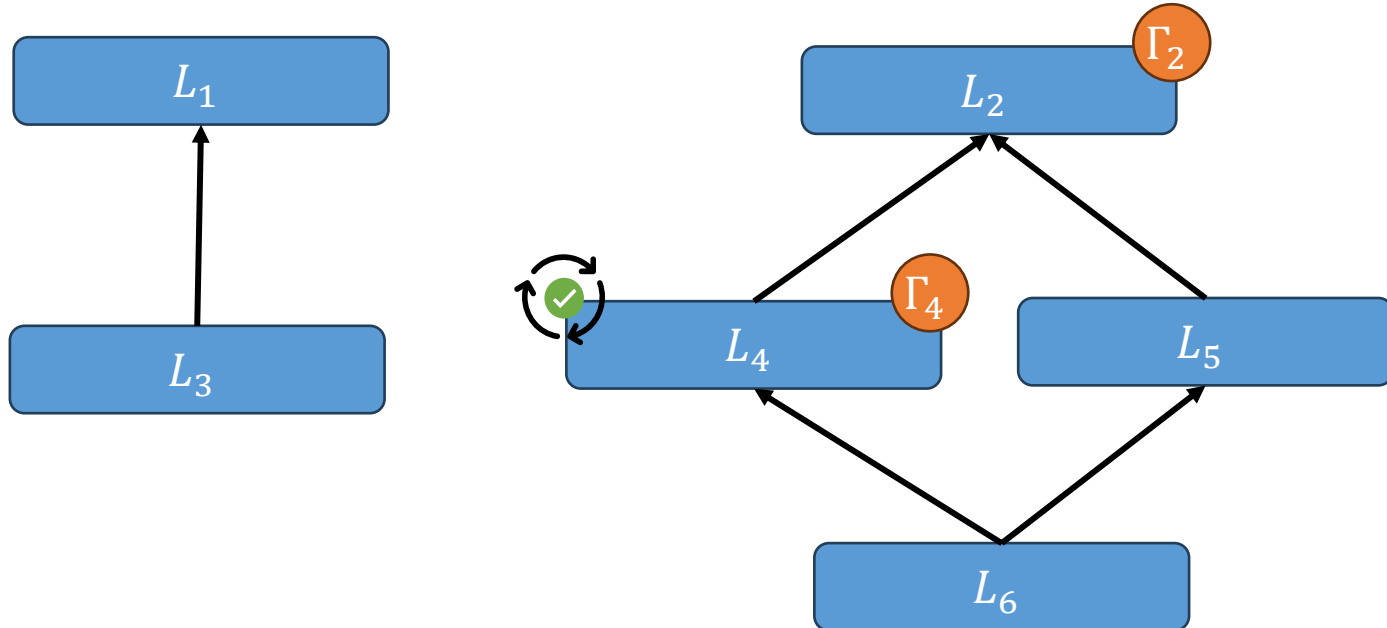
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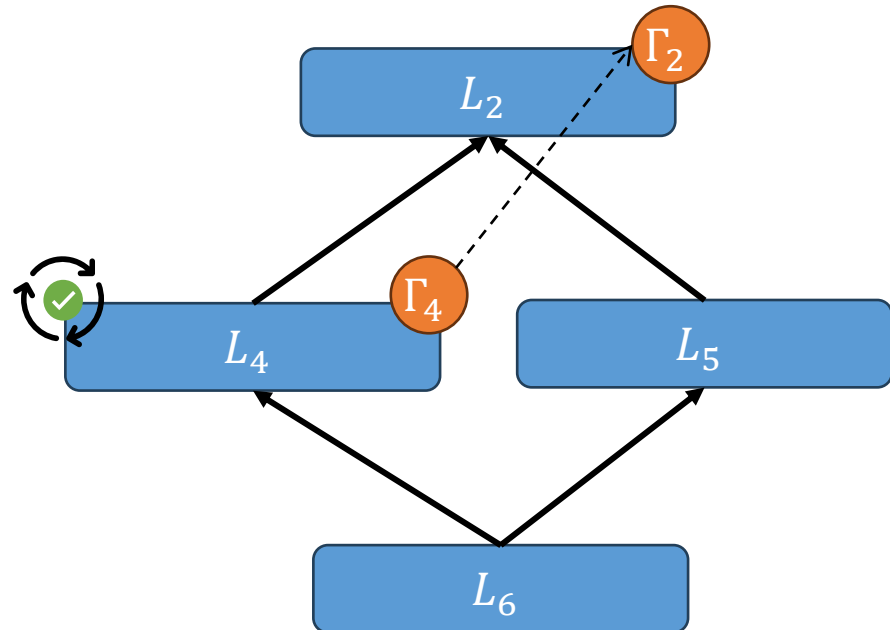
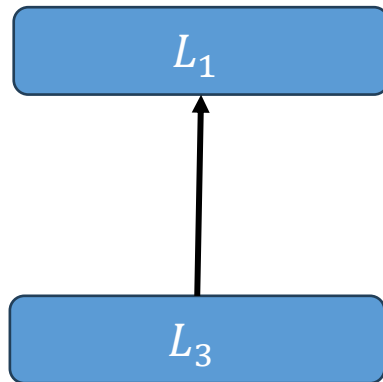
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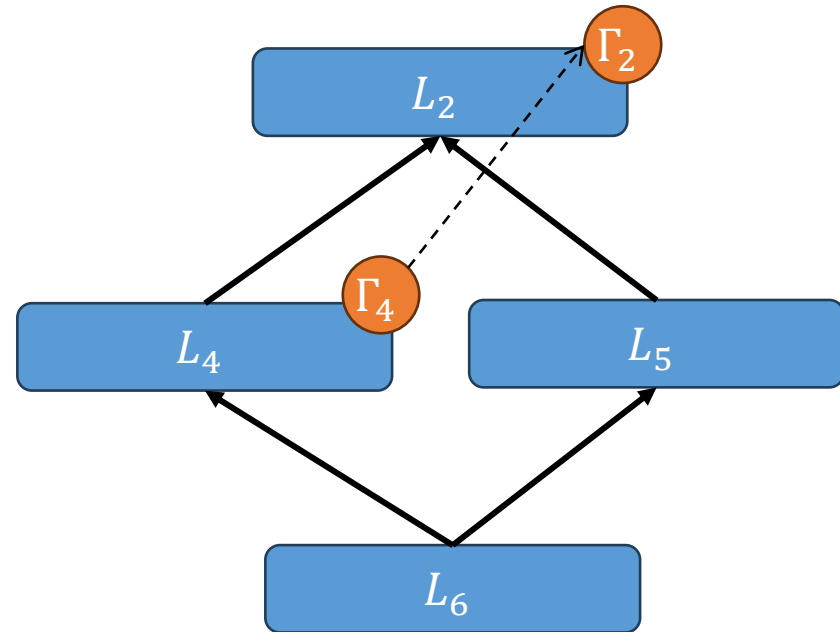
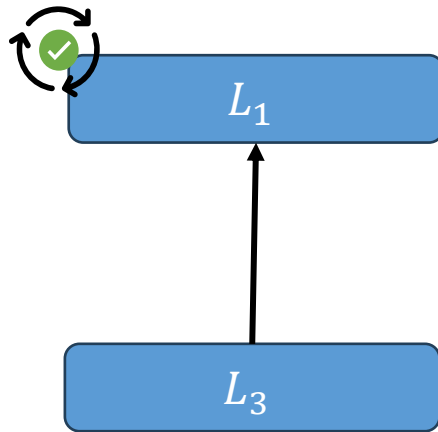
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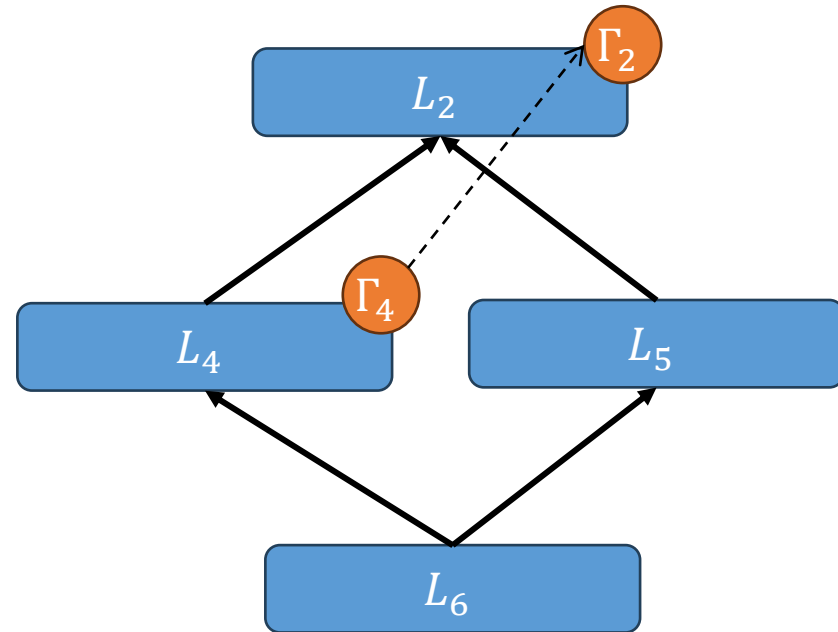
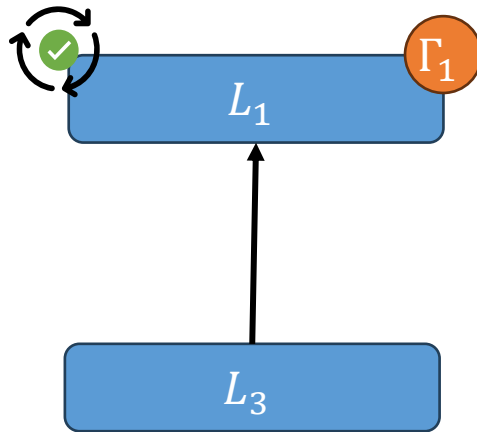
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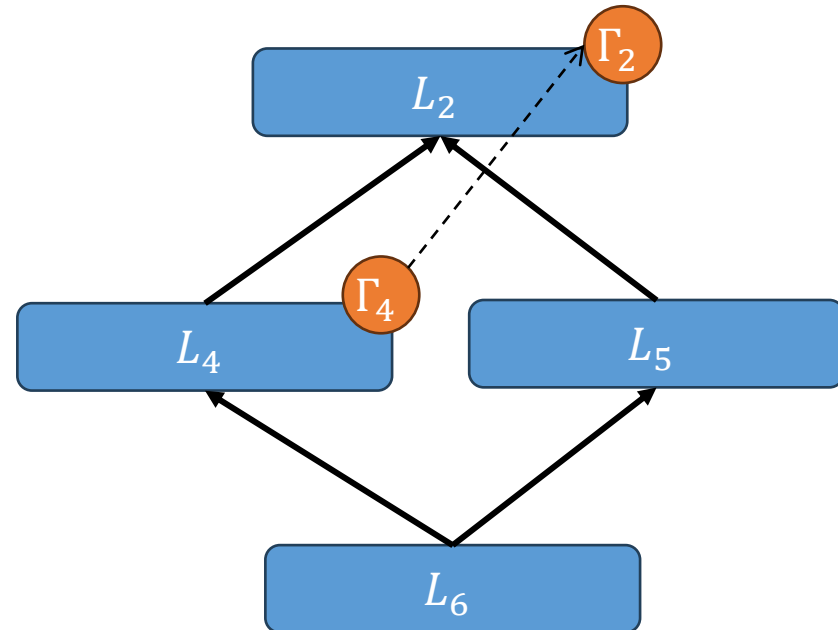
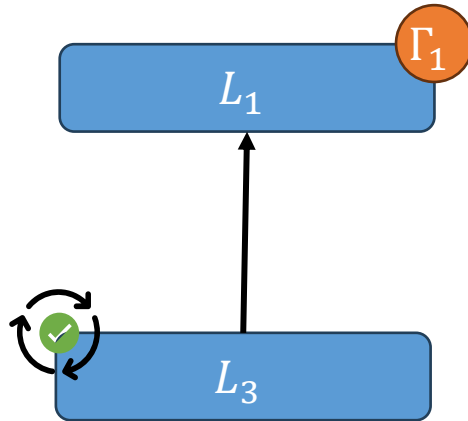
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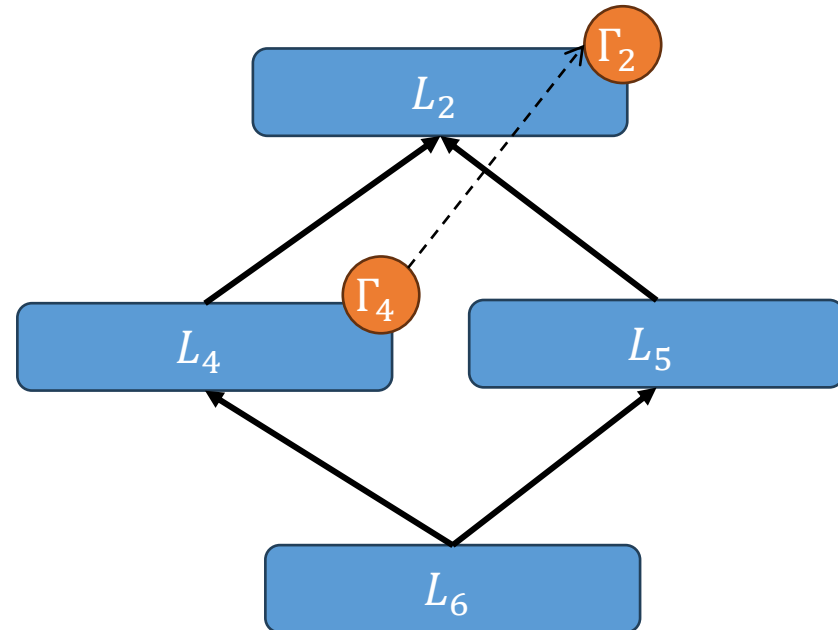
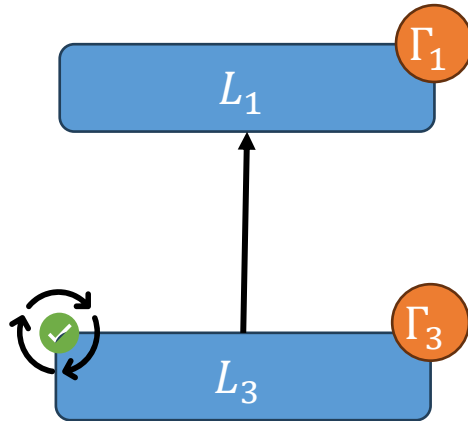
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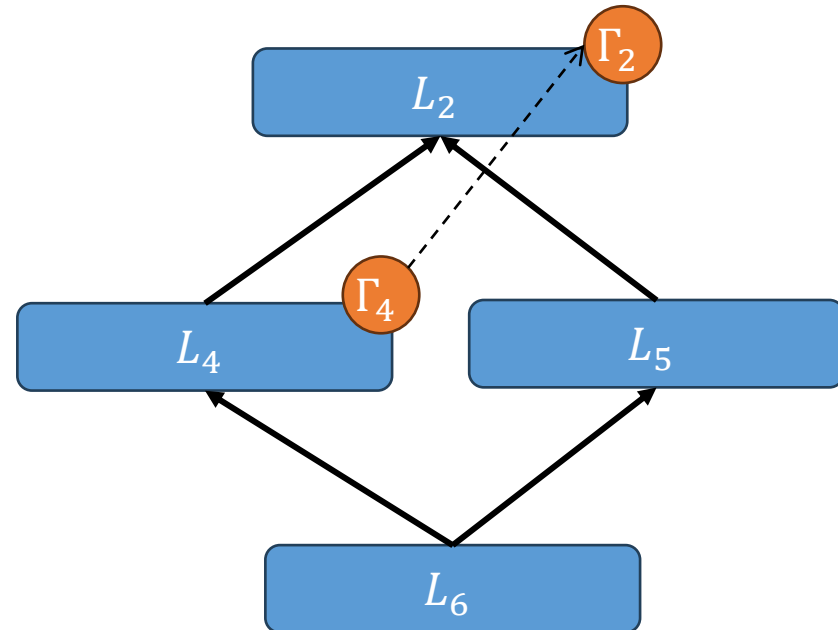
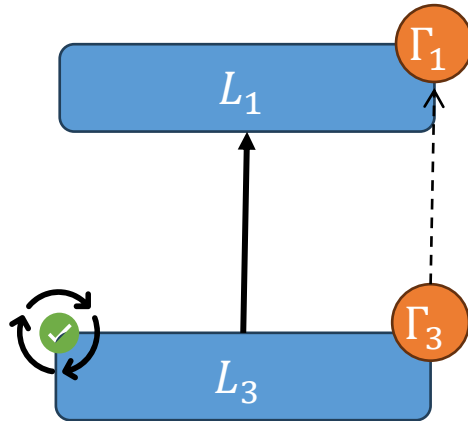
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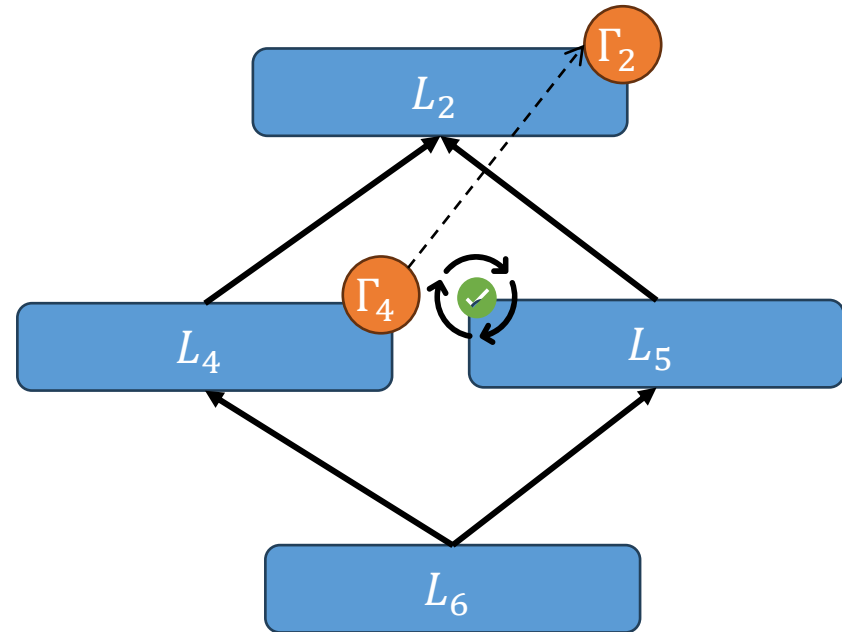
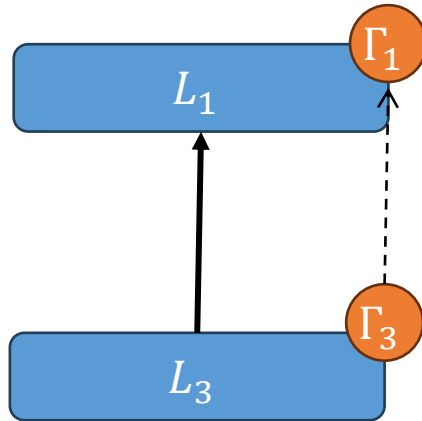
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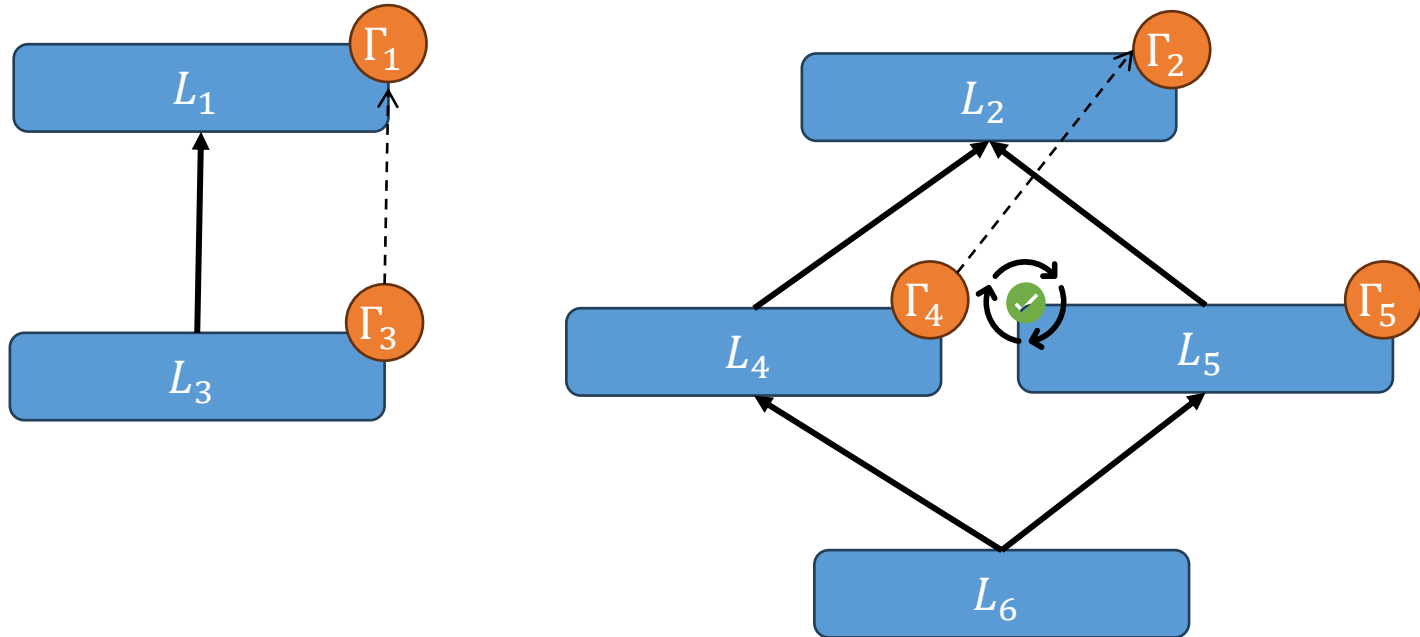
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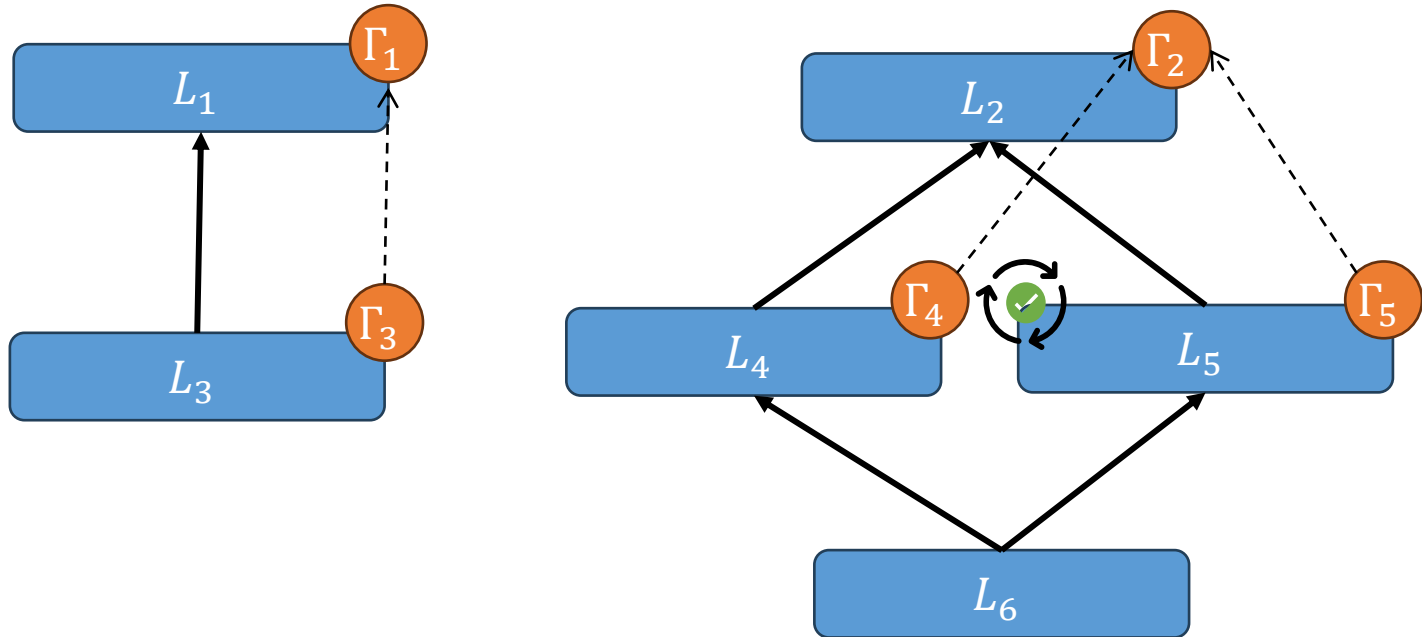
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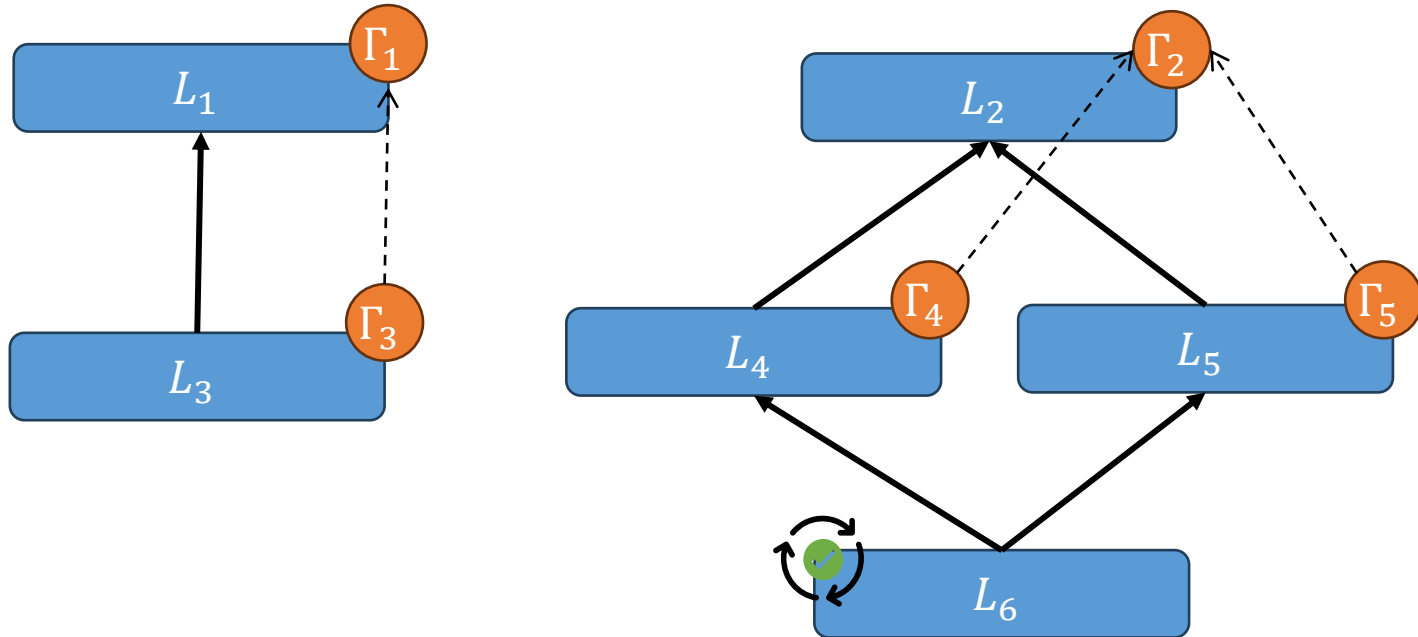
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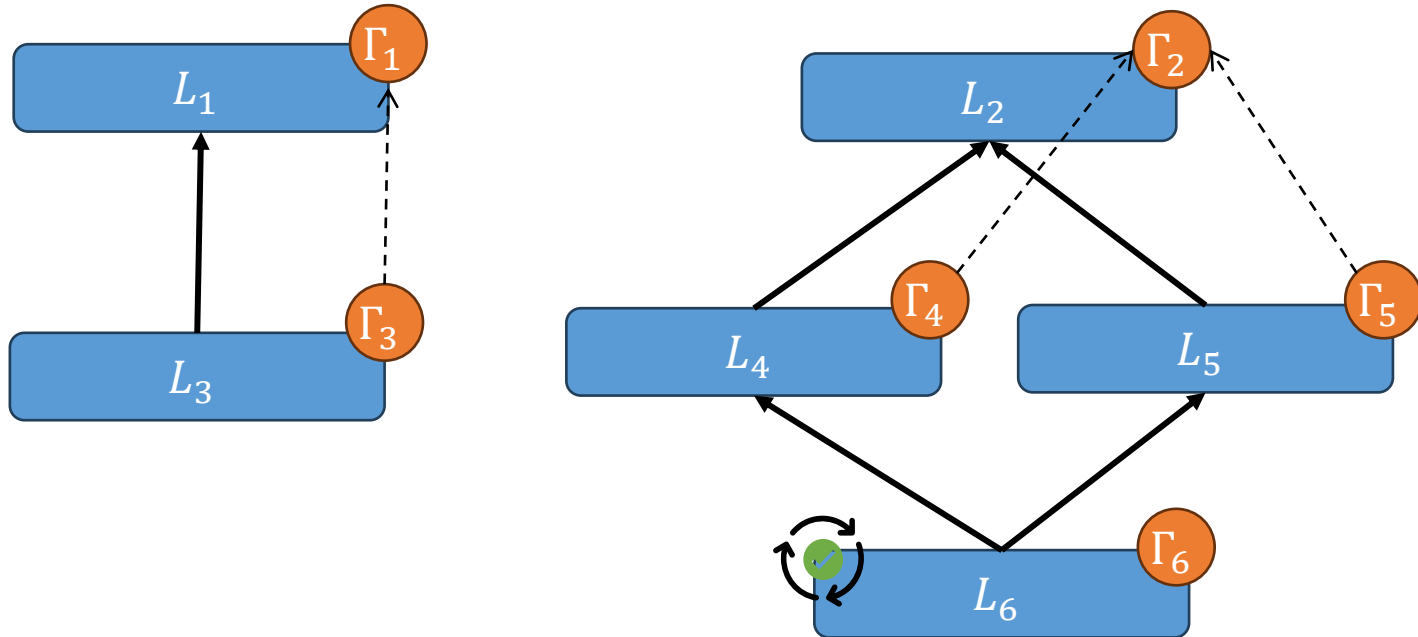
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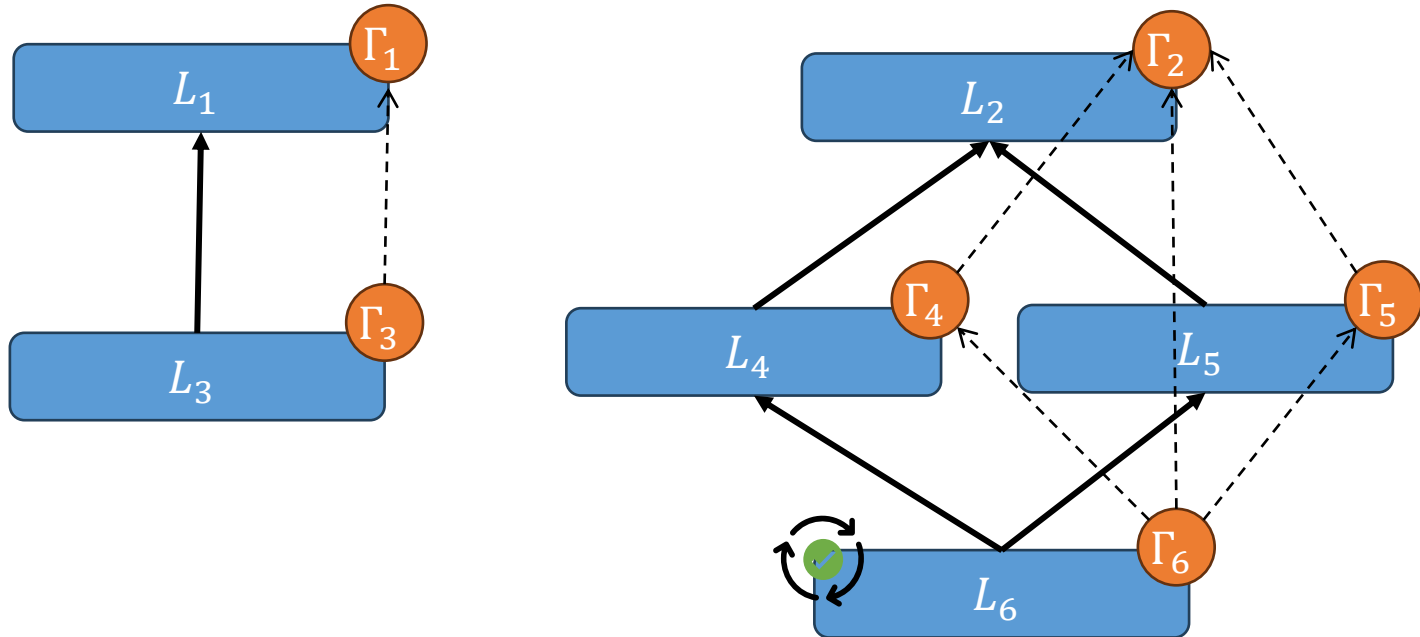
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# LAYERED TYPES – LAYERS

Lukas Abelt, Alcides Fonseca




# LAYEREDTYPES - RESULTS

Lukas Abelt, Alcides Fonseca

- What did we achieve:
  - Prototypical implementation
    - <https://github.com/LuAbelt/LayeredTypes>
  - Example Layers
    - “Normal” Typechecking
    - States
    - Layered Liquid Types
- How far did we get with our vision?

# LAYEREDTYPES – RESULTS

Lukas Abelt, Alcides Fonseca

- Incrementality 
  - Layers are verified independently
- Modularity 
  - Layers may be combined arbitrarily
  - Some restrictions may apply
- Separation of Concerns 
  - Generally yes, but...

```
lukas@DESKTOP-H22A5SC
└─/mnt/c/Projects/LayeredTypes/tests
$ python3 ../main.py -f ../test_code/layers/complex_layers.fl -l ../layer_im
plementations/ -i ../implementations.py -t
Not all layers could be verified.
The following cycle in the layer dependency graph was detected:
  cycleB
  cycleA
The following layers were processed:
A: SUCCESS
B: SUCCESS
C: SUCCESS
D: SUCCESS
cycleA: CYCLE
cycleB: CYCLE
failLayerA: FAILURE
blockedLayerB: BLOCKED
blockedLayerC: BLOCKED
dependOnCycleA: CYCLE_BLOCKED

The following layers failed during typechecking:
failLayerA:
  Layer 'failLayerA' failed with error: Layer A failed
```

# LAYEREDTYPES – ERRORS

Lukas Abelt, Alcides Fonseca

dimensions.fl

```
create :: rows :: { r:Int | r>0 } → { c:Int | true } → {  
    d:DataSet | n_rows(d)==r }  
create :: cols :: { r:Int | true } → { c:Int | c>0 } → {  
    d:DataSet | n_cols(d)==c }  
create :: dims :: { r:Int | true } → { c:Int | true } → {  
    d:DataSet | true }  
  
data :: dims :: { d:DataSet | n_cols(d) ≥ (n_rows(d)*10) }  
data :: rows :: { drf:DataSet | true }  
data :: cols :: { dcf:DataSet | true }  
  
let data := create(5,10) in {  
    data  
}
```

# LAYEREDTYPES – ERRORS

Lukas Abelt, Alcides Fonseca

```
dimensi Lukas@DESKTOP-H22A5SC
create L/mnt/c/Projects/LayeredTypes/tests
$ python3 ../main.py -f dimensions.fl -i ./implementations.py -l ../layer_i {
implementations/ -t
Not all layers could be verified.
create The following layers were processed: {
rows: SUCCESS
cols: SUCCESS
create dims: FAILURE {

The following layers failed during typechecking:
data dims:
data Layer 'dims' failed with error: 9:1: Error during assigning identi
data fier 'data' in let statement:
data { d:DataSet | ((true && (n_rows(d) == create_r)) && (n_cols(d) == create_c)
) } is not a subtype of { d:DataSet | (n_cols(d) ≥ (n_rows(d) * 10)) }
In Context:
let da create_c : { v:Int | ((v == 10) && (v == 10)) && (v == 10)) }
da create_r_1_1 : { v:Int | (v == 5) }
} create_r_1 : { v:Int | (v == 5) }
create_r : { v:Int | ((v == 5) && (v == 5)) && (v == 5)) }
(line 9)
```



# LAYEREDTYPES – FUTURE

Lukas Abelt, Alcides Fonseca

- LayeredTypes should be treated as a prototype/proof-of-concept
  - Not viable for real-world projects
- Future works includes formalization of the approach

# THANKS FOR YOUR ATTENTION!

### MOTIVATION

Lukas Abelt, Alcides Fonseca

- Original Idea comes from challenges in Liquid Types:
  - Composability
  - Reusability
  - Error-Detection

```
Liquid Type  
x :: Int  
-- Do something with x  
x = -10
```

```
Typed  
x :: Int  
x = 100  
-- Do something with x  
x = -10
```

```
Liquid Type  
[-@ x :: { v: Int | v > 0 } @-]  
x :: Int  
x = 100  
-- Do something with x  
x = -10 -- ERROR with Liquid Types
```

This work was supported by Fundação para a Ciência e Tecnologia (FCT) in the LASIGE Research Unit under the ref. UIDB/00408/2020 and UIDP/00408/2020, by the CMU-Portugal project CAMELOT (LISBOA-01-0247-FEDER-045915), and the RAP project under the reference (EXPL/CCI-COM/1306/2021)

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### LAYEREDTYPES – MOTIVATION

Lukas Abelt, Alcides Fonseca

```
Before  
[-@ type OrderedList = { v:[Int] | len(v) > 0  
  && all(i,j | i<j => v[i]<v[j]) } @-]  
[-@ type PositiveList = { v:[Int] | len(v) > 0  
  && all(i | v[i] > 0) } @-]  
  
[-@ foo :: OrderedList -> Int @-]  
foo :: [Int] -> Int  
  
[-@ x :: PositiveList @-]  
x :: [Int]  
  
foo(x) = ... -- Perform some complicated operation
```

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### LAYEREDTYPES – ARCHITECTURE

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